1. (24 points) The following problems are not related. If a limit does not exist, you must say so. If you use a theorem, clearly state its name and show that its hypotheses are satisfied.

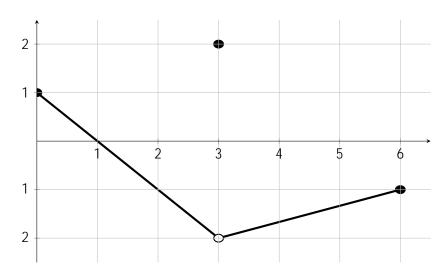
(Reminder: You may not use L'Hôpital's Rule or "Dominance of Powers" in any solutions on this exam.)

(a)
$$\lim_{x \neq 0} \frac{\sec x}{4x \cot 2x}$$

(b)
$$\lim_{x/\sqrt{1}} \frac{\sin^2 x}{x}$$

(c)
$$\lim_{x/1} \frac{x}{2} = \frac{1}{5} \frac{1}{x^2}$$

- 2. (21 points) The following problems are unrelated.
 - (a) Given that $\csc = \sqrt[p]{5}$ and =2 < < <, find the values of tan and $\cos(2)$.
 - (b) Find all values of x in the interval [0]; that satisfy $\tan x \sec x = 4 \sin x$.
 - (c) A squirrel is up a tree, and it sees a peanut on the ground some distance away. If the straight-line distance between the peanut and the squirrel is 50 ft, and the angle between the straight-line and the tree is =6 radians, how far down the tree and across the ground must the squirrel travel to reach the peanut? Give your answer with appropriate units.
- 3. (15 points) Shown below is a graph of y = f(x), which consists of two line segments with a single removable discontinuity.



- (a) Find a formula for f(x).
- (b) Sketch a graph of y = jf(x)j + 1. Label the intercepts, if any.
- (c) Suppose we use the precise definition of a limit to verify the value of $\lim_{x \neq 0} f(x)$, and we find that if 4 < x < 6, then $\frac{5}{3} < f(x) < 1$. What are the corresponding values of and ? (recall the precise definition of a limit: the limit of f(x) as x approaches a is L if for every number > 0, there is a corresponding > 0 such that if 0 < jx aj < j, then jf(x) k = 0.

4. (20 points) Consider the function $g(x) = \frac{2x^2}{x^2} \frac{12x + 16}{7x + 12}$.

(Reminder: You may not use L'Hôpital's Rule or "Dominance of Powers" in any solutions on this exam.)

- (a) Find the domain of g(x). Express your answer in interval notation.
- (b) Find and classify all discontinuities of g(x); justify your answers by calculating the appropriate limits.
- (c) Find the horizontal asymptotes, if any; justify your answers by calculating the appropriate limits.
- 5. (10 points) Consider the function

$$f(x) = \begin{cases} b\cos(x); & x = 1 \\ 3 & 2x = 2; & x > 1 \end{cases}$$

Find the value of b such that $\lim_{x/1} f(x)$ exists. Justify your answer by calculating appropriate limits.

6. (10 points) Show that the equation $x = \sin x \cos x$ has at least one real solution. Indicate the interval where a solution can be found.